## MAGDALEN COLLEGE SCHOOL OXFORD



# 13+ ENTRANCE EXAMINATION 

## SPECIMEN

## MATHEMATICS

Please read this information before the examination starts.

- This examination is 1 hour long.
- Please try all the questions.
- Write your answers in the spaces provided.
- All working should be written on the paper.
- Calculators are allowed.

1. Simplify
a) $3 x+2 y+5 x-3 y$

Answer:.
b) $\quad 2 x^{2}+2 x^{2}$
$\qquad$
c) $\frac{a+a+a}{a}$

Answer:
d) $\frac{x}{3}+\frac{x}{4}$

## Answer:

e) $2 n^{2} k+k^{2} n+3 k n^{2}$
f) $2+5 a-5$
2. Sound travels at 330 metres per second. If thunder is heard 24 seconds after the lighting is seen, how far away is the storm?

Give your answer in km.

Answer:
[2]
3. How many paving stones, each measuring 75 cm by 60 cm , are needed to cover a rectangular courtyard 9 m by 6 m ?

Answer
4. The distance from Oxford to London is 90 km . I travel from Oxford to London at $45 \mathrm{~km} / \mathrm{h}$ as there is a lot of traffic. The road is less congested on the return journey. I calculate that my average speed for the TOTAL journey is $60 \mathrm{~km} / \mathrm{h}$. What was my average speed for the journey from London to Oxford?

Answer:
5. A set of five positive whole numbers has a mean of 6 , a median of 5 and a mode of 4 .

List a set of possible numbers

Answer:
[3]
6. Consider the cube shown below


One face is painted grey, one face has a circular hole cut out of it and one face has a square hole cut out of it. All the other faces of the cube are white and have no holes in them.

Here is a net of the cube.


Draw the circular hole and the square hole on the correct places on the net
7. In each question, find the number that is the odd one out.
a)

$$
2 \times 2 \times 2,3 \times 2,2^{3}
$$

b)
$40 \%, \frac{2}{5}, \frac{40}{10}$

Answer: $\qquad$ [1]

$$
\text { c) } \quad \frac{2}{3}, 60 \%, \frac{6}{10}
$$

d) $\frac{1+1}{1 \times 1}, \frac{2+2}{2 \times 2}, \frac{1+1}{-1 \times-1}$

Answer:
[1]
Answer:.
[1]
8. Here is a diagram of a kite; all measurements are in cm.


Work out the length $h$, giving your answer in millimetres correct to the nearest millimetre.
9. Solve the following equations
a) $\frac{x}{5}=35$

Answer:
b) $\frac{63}{x}=7$

Answer:
c) $\frac{3}{4} x-5=7$

Answer:
d) $\frac{7}{x+1}=3$
10. Consider this diagram which shows four identical circles inside a square of side length 10 cm .


Find the unshaded area.
11. The year 2011 is one where the digits add up to a total of 4 . List the years where this occurred between 1000 and 2000 AD

> Answer:
12.

If:
$A+C=A$
$F \times D=F$
$B-G=G$
$A+H=E$
$B \div H=G$
$E-G=F$
and $A$ to $H$ represent the numbers from 0 to 7 (not necessarily in that order) Find the values of $A, B, C, D, E, F, G$ and $H$.

Answer: A= $\qquad$ $\mathrm{B}=$ $\qquad$ $\mathrm{C}=$ $\qquad$ D= $\qquad$ E= $\qquad$ F= $\qquad$ G= $\qquad$ $\mathrm{H}=$
13. i) Find the values of the angles $a$ and $b$ if :


Answer: $\mathrm{a}=$
[2]


Answer: $\mathrm{b}=$
[3]
14. These are approximate equivalents of some metric and imperial units:

$$
1 \text { metre } \approx 1.1 \text { yards }, \quad 2.5 \mathrm{~cm} \approx 1 \mathrm{inch}, \quad 1 \text { pint } \approx \frac{3}{5} \text { litre }
$$

Answer the following questions using these approximations.
(a) The male shot putt world record stands at 23 metres. What is this record in yards?

Answer
[2]
(b) The world's tallest ever woman was recorded at a height of 250 cm . Given that there are 12 inches in one foot, how tall is this in feet and inches?

Answer.
(c) The average female human's body contains 5.6 litres of blood. When pregnant, the amount of blood in a female's body doubles.
How much blood would the average pregnant human female have in her body in pints?

Answer
15. Solve these equations.
(a) $3 x-7=8$
(b) $2(x-1)=10$

## Answer

(c) $3(2 x-4)=x-7$

Answer
[2]
d) $2(x-3)-(4 x-2)=5$
16.

(a) Describe the single transformation which will take shape A onto shape B.

Answer.
[2]
(b) Describe the single transformation which will take shape A onto shape C .

Answer
(c) If each of the squares on the grid is a square of side length 1 , what is the area of shape A?

## Answer

(d) A new transformation is maps shape A onto shape $D$, and causes all of the lengths of shape A to double.
Write down the area of shape $D$.
17. Leaving your answers as top heavy fractions work out:
(a) $\frac{1}{1+\frac{1}{2}}$.
(b) $\frac{1}{1+\frac{1}{1+\frac{1}{2}}}$
(c) $\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{2}}}}$

Predict the next two answers if the pattern in the question continues in the same way.
18. A polystyrene moulding has a cross section in the shape of a letter L with its longer edges 10 cm and all other measurements 5 cm , including its depth. What is its total surface area?

19. Suppose $x=2, y=0.5$ and $z=-3$.
i) Find the value of
a) $2 x+y$

Answer:
[1]
b) $x+(y-z)$

Suppose $x=2, y=0.5$ and $z=-3$.
c) $x-2(z-y)$
$\qquad$
Answer:
[2]
d) $\frac{x^{2}}{y^{2}}$

20．James and Michael are arguing．James says that
$n^{2}+n+41$ is a prime number for any positive integer $n$ ．He uses the example
When $\mathrm{n}=1, \quad n^{2}+n+41=1+1+41=43$ which is a prime number
Michael is not sure，wants to try out a few more values of n and then wants to think about the problem．
（a）Try $n=2$ ．Is $n^{2}+n+41$ a prime number？

> Answer:
（b）Try $n=3$ ．Is $n^{2}+n+41$ a prime number？
Answer：．．．．．．．．．．．．．．．．．．．．．．．．．「21
（c）Do you think that $n^{2}+n+41$ is a prime number for any value of $n$ ？

Explain your reasoning fully．

